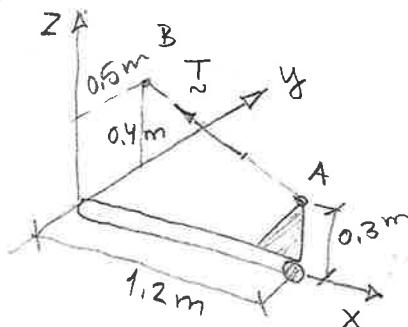


Seminarie pass 6

1)



$$T = 2 \text{ kN}, \quad \vec{T} = T \vec{e}_{AB}$$

$$\vec{AB} = (0, 0.5, 0.4) - (1.2, 0, 0.3)$$

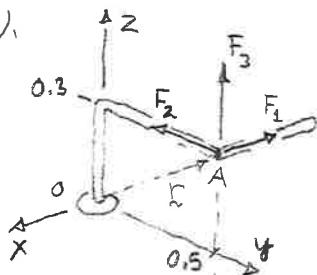
$$= (-1.2, 0.5, 0.1)$$

$$|\vec{AB}| = 1.304 \Rightarrow$$

$$\vec{e}_{AB} = (-0.920, 0.383, 0.0767)$$

DVS $\vec{T} = (-1.84, 0.766, 0.153) \text{ kN}$

2)



Flytta krafterna längs verkningslinjerna så de hamnar i A.

$$\vec{M}_0 = \vec{r} \times \vec{F} \quad \text{med } \vec{r} = \vec{OA}$$

och $\vec{F} = (-F_1, -F_2, F_3)$

Vektorn $\vec{r} = (0, 0.5, 0.3) \text{ (i m)}$ \Rightarrow

$$\vec{M}_0 = \begin{vmatrix} \vec{e}_x & \vec{e}_y & \vec{e}_z \\ 0 & 0.5 & 0.3 \\ -100 & -20 & 30 \end{vmatrix} = \begin{matrix} \vec{e}_x & \vec{e}_y & \vec{e}_z \\ 0 & 0.5 & 0.3 \\ -100 & -20 & 30 \end{matrix} \vec{e}_x - \begin{matrix} \vec{e}_x & \vec{e}_y & \vec{e}_z \\ 0 & 0.5 & 0.3 \\ -100 & -20 & 30 \end{matrix} \vec{e}_y + \begin{matrix} \vec{e}_x & \vec{e}_y & \vec{e}_z \\ 0 & 0.5 & 0.3 \\ -100 & -20 & 30 \end{matrix} \vec{e}_z =$$

$$= \vec{e}_x \cdot 0.5 \cdot 30 + \vec{e}_y \cdot 0.3 \cdot (-100) + \vec{e}_z \cdot 0 +$$

$$- \vec{e}_x \cdot 0.3 \cdot (-20) - \vec{e}_y \cdot 0 - \vec{e}_z \cdot 0.5 \cdot (-100) =$$

$$= (15+6, -30, 50)$$

Alltså $\vec{M}_0 = (21, -30, 50) \text{ Nm}$

2 forts.

Alt. Direkt beräkning

- Krafterna F_1 : moment map $y \perp z$ *

$$\vec{M}_1 = (0, -0.3 \cdot 100, 0.5 \cdot 100) = (0, -30, 50) \text{ Nm}$$

- Krafterna F_2 : moment map x enbart

- $\vec{M}_2 = (0.3 \cdot 20, 0, 0) = (6, 0, 0) \text{ Nm}$

- Krafterna F_3 : moment map x enbart

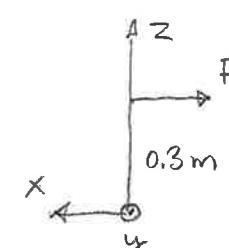
$$\vec{M}_3 = (0.5 \cdot 30, 0, 0) = (15, 0, 0) \text{ Nm}$$

Totalt $\vec{M}_0 = \vec{M}_1 + \vec{M}_2 + \vec{M}_3 = (21, -30, 50) \text{ Nm}$

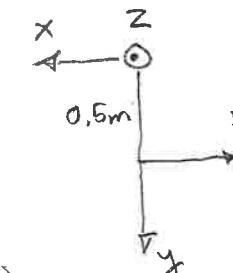
DVS samma svar

*) Projektioner:

F_1 map y

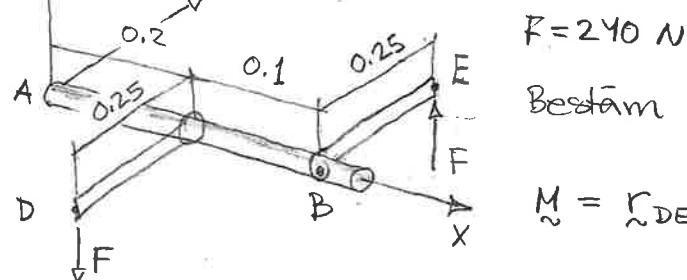
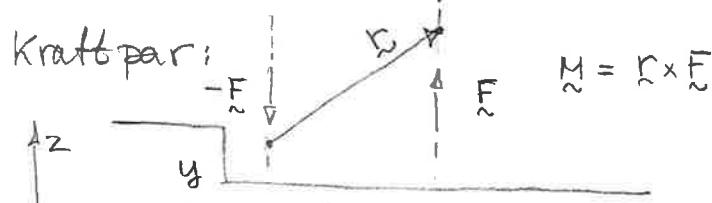


F_1 map z



$$(F_1 = 100 \text{ N})$$

3)



$$\vec{r}_{DE} = (0.1, 0.5, 0) \text{ m}, \vec{F}_{\text{upp}} = (0, 0, 240) \text{ N}$$

$$\vec{M} : \begin{array}{cccccc} \hat{\epsilon}_x & \hat{\epsilon}_y & \hat{\epsilon}_z & \hat{\epsilon}_x & \hat{\epsilon}_y & \hat{\epsilon}_z \\ 0.1 & 0.5 & 0 & 0.1 & 0.5 & 0 \\ 0 & 0 & 240 & 0 & 0 & 240 \end{array} \Rightarrow$$

$$\vec{M} = \hat{\epsilon}_x \cdot 0.5 \cdot 240 - \hat{\epsilon}_y \cdot 0.1 \cdot 240 = (120, -24, 0) \text{ Nm}$$

(Alt.1) Direkt beräkning av kräftparets komponenter

$$\left\{ \text{kring } X: M_x = F \cdot 0.5 \text{ m} = 120 \text{ Nm} \right.$$

$$\left. \text{kring } y: M_y = -F \cdot 0.1 \text{ m} = -24 \text{ Nm} \right.$$

DVS samma resultat

3 forts

Alt.2

Räkna moment map godtycklig plkt för var och en av krafterna
Välj tex plkten B:

$$\begin{aligned} \vec{F}_{\text{ner}} &: (-0.25 \cdot 240, -0.1 \cdot 240, 0) \\ \vec{F}_{\text{upp}} &: (0.25 \cdot 240, 0, 0) \end{aligned} \quad \Rightarrow$$

$$\vec{M} = (0.5 \cdot 240, -24, 0) \quad \text{samma.}$$